

Reaccredited 'A+ 'Grade by NAAC(CGPA:3.68/4.00)

College with Potential for Excellence by UGC

DST-FIST Supported & STAR College Scheme by DBT

## **Faculty of Science**

Bachelor of Science (B.Sc.)

SUBJECT: MATHEMATICS

B.Sc. III Semester Paper- Major/ Minor

Abstract Algebra and Linear Algebra

### **Course Outcomes**

CO.No.	Course Outcomes	Cognitive Level
CO1	Recognize the algebraic structures as a group, and classify them as abelian, cyclic and permutation groups, etc.	U
CO2	Link the fundamental concepts of groups and symmetrical figures.	Ap
CO3	Analyze the subgroups of cyclic groups.	U
CO4	Explain the significance of the notion of cosets, normal subgroups, and quotient groups.	E
CO5	The fundamental concept of rings, fields, subrings, integral domains and the corresponding morphisms	U
CO6	Analyze whether a finite set of vectors in a vector space is linearly independent. Explain the concepts of basis and dimension of a vector space.	U
C07	Understand the linear transformations, rank and nullity, matrix of a linear transformation, algebra of transformations and change of basis.	U
CO8	Compute the characteristic polynomial, eigen values, eigen vectors and eigen spaces, as well as the geometric and the algebraic multiplicities of an eigen value and apply the basic diagonalization result.	Ap

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Credit and Marking Scheme

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	Credits	Ma	ırks	Total Marks
		Internal	External	1000000
Theory	6	40	60	100
Total	6	3110811118	100	

#### **Evaluation Scheme**

	Marks	
	Internal	External
heory	3 Internal Exams of 20 Marks	1 External Exams
	(During the Semester)	(At the End of Semester)
	(Best 2 will be taken)	

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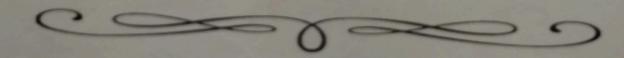
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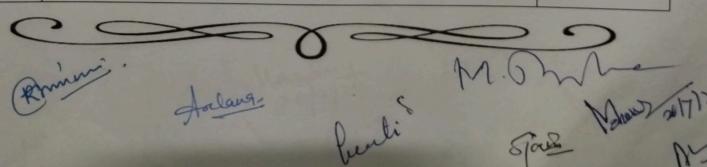
## Content of the Course Theory

No. of Lectures (in hours per week):6 Hrs. per week

Total No.	of Lectures: 90Hrs.	П
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Maximum Marks: 60

1.1 Historical background:  1.1.1 A brief historical back ground of the Algebra in the context of India and Indian heritage and culture  1.1.2 A brief biography of Brahmagupta  1.2 Groups, Subgroups and their basic properties  1.3 Cyclic groups  1.4 Coset decomposition  1.5 Lagrange's and Fermat's theorem  1.6 Normal subgroups  1.7 Quotient groups  2.1 Homomorphism, Kernel of homomorphism and Isomorphism of groups  1.2 Fundamental theorem of homomorphism  2.3 Transformation and permutation group Sn (n<5)  2.4 Cayley's theorem  2.5 Group automorphism  2.6 Inner automorphism  2.7 Group of automorphisms  3.1 Definition and basic properties of rings  3.2 Ring homomorphism  3.3 Subring	60
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3.8 Field	
4.1 Definition and examples of Vector space	THE PERSON NAMED IN
4.2 Subspaces	4
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	4.3 Sum and direct sum of subspaces 4.4 Linear span, Linear dependence, linear independence and	
IV	their basic properties	284
	4.5 Basis	347733
	4.6 Finite dimensional vector space and dimension	150/2011
	4.6.1 Existence theorem	
	. 4.6.2 Extension theorem	Part Part Control
	4.6.3 Invariance of the number of elements	3 330 3
	4.7 Dimension of sum of subspaces	
	4.8 Quotient space and its dimension	
	5.1 Linear transformation and its representation as a matrix	
	5.2 Algebra of linear transformation	
	5 2 Pank-Nullity theorem	24
	5.4 Change of basis, dual space, bi-dual space and natural	-
V	isomorphism	
	5.5 Adjoint of a linear transformation	
300	5.6 Eigen values and Eigen vectors of a linear transformation	
	Diagonalization	

### References

#### **Text Books:**

- 1. I.N.Herstein:Topics in Algebra, Wiley Eastern Ltd. New Delhi.1977.
- 2. K. B. Datta: Matrix and Linear Algebra, Prentice Hall of India Pvt. Ltd. New Delhi.
- 3. Gerard G. Emch, R. Sridharan and M.D. Srinivas: Contributions to the History of Indian Mathematics, Hindustan Book Agency, Vol.3,2005.
- 4. मध्यप्रदेशहिंदीग्रंथअकादमीकीपुस्तके।

### Reference Books:

- 1. Surjeet Singh and Qazi Zameeruddin: Modern Algebra, Vikas Publishing House Pvt Ltd; Eighth edition, 2006.
- 2. N. Jacobson: Basic Algebra. Vol. I and II, W. II Freeman, 1980.
- 3. I.S. Luther and I.B.S. Passi: Algebra. Vol. I and II, Narosa Publishing House, 1997.
- 4. Shanti Narayan: A text Book of Modern Abstract Algebra, S. Chand and Company.
- 5. A.K. Vasishtha and A.R. Vasishtha: Modern Algebra, Krishna Publication; 68th
- 6. K.Hoffiman and R. Kunze: Linear Algebra. 2<sup>nd</sup> Edition, Prentice Hall Engle wood Cliffs, New Jersey, 1971.
- 7. A.R. Vasishtha and J.N. Sharma: Linear Algebra, Krishna Prakashan Media

